Chapter 27. Graphical Solution (Solution of Simultaneous Linear Equations, Graphically)

Exercise 27(A)

Solution 1:

(i)

The graph x = 5 in the following figure is a straight line AB which is parallel to y axis at a distance of 5 units from it.



(ii) x+5=0 x = -5

The graph x = -5 in the following figure is a straight line AB which is parallel to y axis at a distance of 5 units from it in the negative x direction.











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(iv) y + 7 = 0 y = -7

The graph y = -7 in the following figure is a straight line AB which is parallel to x axis at a distance of 7 units from it in the negative y direction.





 $\therefore y = \frac{6-3x}{2}$ When x=0; y = $\frac{6-3x0}{2} = \frac{6-0}{2} = 3$ When x=2; y = $\frac{6-3x2}{2} = \frac{6-6}{2} = 0$ When x=4; y = $\frac{6-3x4}{2} = \frac{6-12}{2} = -3$ $\boxed{x \ 0 \ 2 \ 4}$ y 3 0 -3

Plotting these points we get the required graph as shown below:



x-5y+4=0

⇒ 5y=4+x

$$\therefore y = \frac{x+4}{5}$$

When x=1; $y = \frac{1+4}{5} = \frac{5}{5} = 1$
When x=6; $y = \frac{6+4}{5} = \frac{10}{5} = 2$
When x=-4; $y = \frac{-4+4}{5} = \frac{0}{5} = 0$
 $x = \frac{16}{5} = \frac{10}{5} = 0$

Plotting these points we get the required graph as shown below:



(viii)

5x + y + 5 = 0

⇒y=-5x-5

When $x=0; y = -5 \times x - 5 = -0 - 5 = -5$ When $x=-1; y = -5 \times (-1) - 5 = 5 - 5 = 0$ When $x=-2; y = -5 \times (-2) - 5 = 10 - 5 = 5$

X	0	-1	-2	
У	-5	0	5	

Plotting these points we get the required graph as shown below:



Solution 2:

(i) $\frac{1}{3}x + \frac{1}{5}y = 1$ $\Rightarrow \frac{5x + 3y}{15} = 1$ $\Rightarrow 5x + 3y = 15$ $\Rightarrow 3y = 15 - 5x$ $\Rightarrow y = \frac{15 - 5x}{3}$ When $x = 0; y = \frac{15 - 5 \times 0}{3} = \frac{15 - 0}{3} = 5$ When $x = 3; y = \frac{15 - 5 \times 3}{3} = \frac{15 - 15}{3} = 0$ When $x = -3; y = \frac{15 - 5 \times (-3)}{3} = \frac{15 + 15}{3} = 10$ $\frac{x + 0 + 3 - 3}{y + 5 + 0 + 0}$

Plotting these points we get the required graph as shown below :

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From the figure it is clear that, the graph meets the coordinate axes at (3, 0) and (0, 5)

(ii)
$$\frac{2x+15}{3} = y-1$$

 $\Rightarrow 2x+15=3(y-1)$
 $\Rightarrow 2x+15=3y-3$
 $\Rightarrow 2x-3y=-15-3$
 $\Rightarrow 2x-3y=-18$
 $\Rightarrow -3y=-18-2x$
 $\Rightarrow y=\frac{-18-2x}{-3}$
When $x=0, y=\frac{-18-[2\times 0]}{-3}=\frac{-18-0}{-3}=6$
When $x=-3, y=\frac{-18-[2\times (-3)]}{-3}=\frac{-18+6}{-3}=4$
When $x=-6, y=\frac{-18-[2\times (-6)]}{-3}=\frac{-18+12}{-3}=2$
 $\frac{x \ 0 \ -3 \ -6}{y \ 6 \ 4 \ 2}$
Plotting these points we get the

required graph as shown below :

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From the figure it is clear that, the graph meets the coordinate axes at (-9, 0) and (0, 6)

Solution 3: 4x - 3y + 36 = 0

 $\Rightarrow 4x - 3y = -36$ $\Rightarrow -3y = -36 - 4x$ $\Rightarrow 3y = 36 + 4x$ $\Rightarrow y = \frac{36 + 4x}{3}$ When x = -6, $y = \frac{36 + 4 \times (-6)}{3} = \frac{36 - 24}{3} = 4$ When x = -3, $y = \frac{36 + 4 \times (-3)}{3} = \frac{36 - 12}{3} = 8$ When x = -9, $y = \frac{36 + 4 \times (-9)}{3} = \frac{36 - 36}{3} = 0$ $\boxed{\times -9 - 3 - 6}$ $\boxed{y - 0 - 8 - 4}$

Plotting these points we get the required graph as shown below:

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The straight line cuts the co-ordinate axis at A(0, 12) and B(-9, 0).

:. The triangle $\triangle AOB$ is formed. Area of the triangle $AOB = \frac{1}{2} \times AO \times OB$ $= \frac{1}{2} \times 12 \times 9$ = 54 sq. units :. Area of the triangle is 54 sq. units



Solution 4:

$$2x - 3y - 5 = 0$$

$$\Rightarrow 2x = 3y + 5$$

$$\Rightarrow x = \frac{3y + 5}{2}$$

When $y = 1$, $x = \frac{3(1) + 5}{2} = \frac{8}{2} = 4$
When $y = 3$, $x = \frac{3(3) + 5}{2} = \frac{9 + 5}{2} = 7$
When $y = -1$, $x = \frac{3(-1) + 5}{2} = \frac{5 - 3}{2} = 1$
 $\boxed{x \ 4 \ 7 \ 1}$
 $y \ 1 \ 3 \ -1$

Plotting these points we get the required graph as shown below :



The value of x, when y=7: We have the equation of the line as $x = \frac{3y + 5}{2}$ Now substitute y=7 and $x=x_1$: $x_1 = \frac{3(7) + 5}{2} = \frac{21 + 5}{2} = \frac{26}{2} = 13$ The value of x, when y = -5: Now substitute y=-5 and $x=x_2$: $x_2 = \frac{3(-5)+5}{2} = \frac{-15+5}{2} = \frac{-10}{2} = -5$ Solution 5: 4x + 3y + 6 = 0 $\Rightarrow 3v = -4x - 6$ $\Rightarrow y = \frac{-4x-6}{2}$ When x = 0, $y = \frac{-4(0)-6}{2} = \frac{-6}{2} = -2$ When x = 3, $y = \frac{-4(3)-6}{3} = \frac{-12-6}{3} = -6$ When x = -3, $y = \frac{-4(-3)-6}{3} = \frac{12-6}{2} = 2$ 3 -3 -6 2 Х 0 -6 -2 V

Plotting these points we get the required graph as shown below:



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The value of y, when x=12: We have the equation of the line as $y = \frac{-4x-6}{3}$ Now substitute x=12 and y=y_1: $y_1 = \frac{-4(12)-6}{3} = \frac{-48-6}{3} = \frac{-54}{3} = -18$ The value of y, when x=-6: Now substitute x=-6 and y=y_2: $y_2 = \frac{-4(-6)-6}{3} = \frac{24-6}{3} = \frac{18}{3} = 6$

Solution 6:

The table is:

Х	-5	-1	3	Ь	13
у	-2	а	2	5	7

Plotting the points as shown in the above table, we get the following required graph:



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Solution 7:

The table is:

X	a	3	-5	5	С	-1
y	-1	2	Ь	3	4	0

Plotting the points as shown in the above table, we get the following required graph:



```
When y = -1, then x = -3
  ⇒a=-3
  When x = -5, then y = -2
  ⇒b=-2
  When y = 4, then x = 7
  \Rightarrow c = 7
Let y=px+q ....(1)
be a linear relation between x and y
Substitute x = -3 and y = -1 in the equation (1), we have,
-1 = -3p + q \dots (2)
Substitute x = -5 and y = -2 in the equation (1), we have,
-2=-5p+q ....(3)
Subtracting (3) from (2), we have,
1=2p
\Rightarrow p = \frac{1}{2}
From (3), we have,
-2=-5p+q
\Rightarrow -2 = -5\left(\frac{1}{2}\right) + q
\Rightarrow -4 = -5 + 2q
\Rightarrow 2q = 5 - 4
\Rightarrow 2q = 1
\therefore q = \frac{1}{2}
Thus, the linear relation is
y=px+q
\Rightarrow y=\frac{1}{2}x + \frac{1}{2}
\Rightarrow y = \frac{x+1}{2}
```



Solution 8:

The table is:

X	2	3	5	m
У	4	n	-2	-4

Plotting the points as shown in the above table, we get the following required graph:



Plotting the points in the graph we get the above required graph.

Now draw a line x=3, parallel to y-axis to meet the line It meets the line at y=2 and therefore, n=2Now draw a line y=-4, parallel to x-axis to meet the line It meets the line at x=6 and therefore, m=6Thus the values of m and n are 6 and 2 respectively.

Solution 9:

Consider the equation

x - 3y = 18 $\Rightarrow -3y = 18 - x$ $\Rightarrow 3y = x - 18$ $\Rightarrow y = \frac{x - 18}{3}$ The table for x - 3y = 18 is

Х	9	0	6	3
У	-3	-6	-4	-5

Plotting the above points, we get the following required graph:



From the above figure, we have m=3 and n=-4

Solution 10:

(i)

2x + 3y = 1 $\Rightarrow 3y = 1 - 2x$ $\Rightarrow y = \frac{1 - 2x}{3}$

The table for 2x + 3y = 1 is

Plotting the above points in a graph, we get the following graph:



From the above graph, it is clear that k=5

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(ii)

x - 2y + 1 = 0 $\Rightarrow 2y = x + 1$ $\Rightarrow y = \frac{x + 1}{2}$ The table for x - 2y + 1 = 0 is $\boxed{x + 1} = 3$

Х	1	3	5
y	1	2	З

Plotting the above points in a graph, we get the following graph:



From the above graph, it is clear that k - 2=3 ⇒ k=5

Exercise 27(B)

Solution 1:

(i) $x-5=0 \Rightarrow x=5$ $y+4=0 \Rightarrow y=-4$ Following is the graph of the two equations x=5 and y=-4:



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(ii)

 $2x + y = 23 \Rightarrow y = 23 - 2x$ The table for y = 23 - 2x is

×	5	10	15
У	13	3	-7
- 7			

Also, we have 4x - y = 19 $\Rightarrow y = 4x - 19$ The table for y = 4x - 19 is

×	3	4	6
ÿ.	-7	-3	5

Plotting the points we get the following required graph:



From the above graph, it is dear that the two lines y=23-2x and y=4x-19 intersect at the point (7,9)

(iii)

$$3x + 7y = 27 \Rightarrow 3x = 27 - 7y$$

$$\Rightarrow x = \frac{27 - 7y}{3}$$
The table for $3x + 7y = 27$ is

$$\boxed{x 9 2 -5}$$

$$y 0 3 6$$
Also, we have
 $8 - y = \frac{5}{2}x$

$$\Rightarrow x = (8 - y) \times \frac{2}{5}$$

The table for 5x + 2y = 16 is

×	2	4	0
Ŷ.	3	-2	8

Plotting the points we get the following required graph:





From the above graph, it is dear

that the two lines 3x + 7y = 27 and $8 - y = \frac{5}{2}x$

intersect at the point (2,3)

(iv)



$$\frac{x+1}{4} = \frac{2}{3}(1-2y)$$

$$\Rightarrow \frac{x+1}{4} = \frac{2}{3} - \frac{4y}{3}$$

$$\Rightarrow 12 \times \frac{x+1}{4} = 12 \times \frac{2}{3} - 12 \times \frac{4y}{3}$$

$$\Rightarrow 3(x+1) = 8 - 16y$$

$$\Rightarrow 3x + 3 = 8 - 16y$$

$$\Rightarrow 3x + 3 - 8 = -16y$$

$$\Rightarrow 3x - 5 = -16y$$

$$\Rightarrow x = \frac{5 - 16y}{3}$$

× 7 -9 23 y -1 2 -4	The	e tab	le fo	or <u>-</u>	+ 1 4	= ² /3(1 – 1	2y)	is
y -1 2 -4	Х	7	-9	23					
	y.	-1	2	-4					

$$\frac{2+5y}{3} = \frac{x}{7} - 2$$

$$\Rightarrow 21 \times \frac{2+5y}{3} = 21 \times \frac{x}{7} - 21 \times 2$$

$$\Rightarrow 7(2+5y) = 3x - 42$$

$$\Rightarrow 14+35y = 3x - 42$$

$$\Rightarrow 3x = 14+35y + 42$$

$$\Rightarrow 3x = 56 + 35y$$

$$\Rightarrow x = \frac{56+35y}{3}$$



The table for
$$\frac{2+5y}{3} = \frac{x}{7} - 2$$
 is

×	7	-28	42
У	-1	-4	2

Plotting the points we get the following required graph:



From the above graph, it is dear that the two lines $\frac{x+1}{4} = \frac{2}{3}(1-2y)$ and $\frac{2+5y}{3} = \frac{x}{7} - 2$ intersect at the point (7, -1)

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Solution 2:

x - 2y - 4 = 0 $\Rightarrow x = 2y + 4$ The table for x - 2y - 4 = 0 is

×	4	6	2
Y.	0	1	-1

Also we have

2x+y=3 ⇒ 2x=3 - v

$$\Rightarrow 2x = 3 - y$$

 $\Rightarrow x = \frac{3 - y}{2}$

$$\Rightarrow x = \frac{y}{2}$$

The table for 2x+y=3 is

Х	1	0	2
y	1	3	-1

Plotting the above points we get the following required graph:



From the above graph, it is dear that the two lines x - 2y - 4 = 0 and 2x+y=3 intersect at the point (2, -1)

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Solution 3:

2x - y - 1 = 0
$\Rightarrow 2x = y + 1$
$\Rightarrow x = \frac{y+1}{2}$
The table for $2x - y - 1 = 0$ is
× 2 1 0 y 3 1 -1
Also we have
2x+y=9
$\Rightarrow 2x=9-y$
$\Rightarrow x = \frac{9 - y}{2}$
The table for 2x+y=9 is

Plotting the above points we get the following required graph:



From the above graph, it is dear that the two lines 2x - y - 1 = 0 and 2x+y=9intersect at the point (2.5,4)

Solution 4:

3x + 5y = 12 \Rightarrow 3x = 12 - 5y $\Rightarrow x = \frac{12 - 5y}{3}$ The table for 3x + 5y = 12 is Х 4 -1 -6 0 3 У -1 Also we have 3x - 5y + 18 = 0⇒3×= 5y - 18 $\Rightarrow x = \frac{5y - 18}{3}$

The table for 3x - 5y + 18 = 0 is

Х	-6	4	-1
y	0	6	З

Plotting the above points we get the following required graph:



From the above graph, it is dear that the two lines 3x + 5y = 12 and 3x - 5y + 18 = 0intersect at the point (-1,3)

Solution 5:

(i) x + y + 3 = 0 $\Rightarrow x = -3 - y$ The table for x + y + 3 = 0 is 1 0 -2 Х -4 -3 -1 У Also we have 3x - 2y + 4 = 0 \Rightarrow 3x= 2y - 4 $\Rightarrow x = \frac{2y - 4}{3}$ The table for 3x - 2y + 4 = 0 is

×	0	-2	- 43
Y.	2	-1	1

Plotting the above points we get the following required graph:





(ii)

From the above graph, it is clear that the two lines x + y + 3 = 0 and 3x - 2y + 4 = 0intersect at the point (-2, -1)(iii)

Applying Pythagoras Theorem, the distance from the origin $= \sqrt{(-2-0)^2 + (-1-0)^2}$ $= \sqrt{2^2 + 1^2}$ $= \sqrt{4+1}$ $= \sqrt{5}$ = 2.2 cm (approx)

Solution 6:

y - 2 = 0 $\Rightarrow y = 2$ y + 1 = 3(x - 2) $\Rightarrow y + 1 = 3x - 6$ $\Rightarrow y = 3x - 6 - 1$ $\Rightarrow y = 3x - 7$ The table for y + 1 = 3(x - 2) is

×	1	2	З
У	-4	-1	2

Also we have

- x+2y=0
- $\Rightarrow x = -2y$

The table for x + 2y = 0 is

Х	-4	4	-6
Ÿ.	2	-2	3

Plotting the above points we get the following required graph:



The area of the triangle ABC = $\frac{1}{2} \times AB \times CD$ = $\frac{1}{2} \times 7 \times 3$ = $\frac{21}{2}$

(ii)

The coordinates of the vertices of the triangle are (-4, 2), (3, 2) and (2, -1)

= 10.5 sq.units

Solution 7:

 $3x+y+5=0 \Rightarrow y=-3x-5$ The table of 3x+y+5=0 is -3 -2 X 1 -8 4 1 Y $3y - x = 5 \Rightarrow x = 3y - 5$ The table of 3y - x = 5 is -2 1 Х 7 1 2 4 Y 2x + 5y = 1 $\Rightarrow 2x = 1 - 5y \Rightarrow x = \frac{1 - 5y}{2}$ The table of 2x + 5y = 1 is

×	3	-/	-2
Y	-1	3	1
_			

Plotting the above points, we get the following required graph:



The graph shows that the lines of these equations are concurrent.

Solution 8:

$$6y = 5x + 10$$

$$\Rightarrow y = \frac{5x + 10}{6}$$

The table of $6y = 5x + 10$ is

$$\boxed{x \mid 4 \mid -2 \mid -8}$$

<u>^</u>	4	-2	-0
Υ.	5	0	-5

Also, we have

y=5x - 15

The table of y = 5x - 15 is

Plotting the points in a graph, we get the following graph.



(i)

The two lines intersect at (4,5):: AD \perp BC AD = 5 units and BC=5 units

(ii)

The area of the triangle = $\frac{1}{2} \times BC \times AD$ = $\frac{1}{2} \times 5 \times 5$ = $\frac{25}{2}$ sq.units = 12.5 sq.units

Solution 9:

Given that C.P. is 50+3x

Table of C.P

X	0	10	20	30	40	50	60
C.P	50	80	110	140	170	200	230

and S.P. =4x

: Table of S.P.

X	0	10	20	30	40	50	60
S.P	0	40	80	120	160	200	240

Now plotting the points on a graph and we get the following required graph:



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(i)

No. of articles to be manufactured and sold are 50 when there is no loss and no profit.

C.P = S.P = Rs.200 (ii) (a) On article 30, C.P = Rs.140 and S.P. = 120 Therefore Loss = 140 - 120 = Rs.20 (b) On article 60, C.P.=Rs.230 and S.P.= Rs.240 Therefore Profit = 240 - 230 = Rs.10



Solution 10:

2	1-	- ×	= 8	;			
٧÷	_	8+: 2	<u>×</u> ;				
Tł	he	e ta	ble	of 2	y - x	:= {	3 is
	<	-6	-2	2 0	7		
5	/	1	3	4	1		
5y	<u>_</u> -	- x	= 14	1⇒	x = 5	5y -	14
Tł	he	e ta	ble	of x	= 5y	- 1	4 is
	<	-9	-4	- 1	1		
Ŋ	/	1	2	3			
y	_	2x	= 1 :	⇒y	= 1 -	+ 2x	
Tł	he	e ta	ble	ofy	- 2x	= 1	is
>	<	2	-2	0			
Ŋ	/	5	-3	1			

Now plotting the points on a graph and we get the following required graph:



Thus, the vertices of the triangle \triangle ABC are: A(-4,2), B(1,3) and C(2,5)

Solution 11:

X +	· Y =	= 0						
y=	- ×	;						
Th	e ta	ble	of >	(+	y :	= C) is	5
X	5	2	2 -	5				
У	-5	; -	2 5	5				
3х	- 2)	/ =	10 =	⇒,	× =	10) + 3	<u>2y</u>
Th	e ta	ble	of 3	3 <i>x</i>	- 2	<u>y</u>	= 1	0 is
X	4	6	2					
У	1	4	-2					

Now plotting the points on a graph and we get the following required graph:



The two lines intersect at (2, -2):: x = 2 and y = -2

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Solution 12:

x + 2y = 4										
⇒>	<=4	1-2	2y							
The table of $x + 2y = 4$ is										
\times	2	-4	12							
Ŷ.	1	4	-4							
$3x - 2y = 4 \Rightarrow x = \frac{4 + 2y}{3}$										
The table of $3x - 2y = 4$ is										
×	2	4	6							
Ÿ.	1	4	7							

Now plotting the points on a graph and we get the following required graph:



Therefore the solution of the given system of equations is (2,1).

Thus the vertices of the triangle are: A(2,1), B($\frac{4}{3}$, 0) and C(4,0) AD \perp BC and D = (2,0) \therefore AD = 1 and BC=2 $\frac{2}{3}$ units= $\frac{8}{3}$ units Area of the triangle ABC= $\frac{1}{2} \times AD \times BC$ $= \frac{1}{2} \times 1 \times \frac{8}{3}$ $= \frac{4}{3}$ sq.units $= 1\frac{1}{3}$ sq.units





Solution 13:

$$y = \frac{3x + 2}{2}$$

The table for $y = \frac{3x + 2}{2}$ is
 $\frac{x + 2}{2} = \frac{3}{2}$
 $\frac{x + 2}{2} = \frac{3}{2}$
 $\frac{x + 2}{2}$
 $y = \frac{3}{4}x - 2$
The table for $y = \frac{3}{4}x - 2$ is
 $\frac{x + 4}{2} = \frac{3}{4}$

Now plotting the points on a graph and we get the following required graph:



Thus the value of 'x' is -4.

Solution 14:

-2

У

4

2

2x -	+ Зу	= 4					
⇒>	< = _	1-3 <u>)</u> 2	<u>/</u>				
The	e tab	le fo	or 2	X +	Зу	= 4	is
×	-1	-4	5	1			
ÿ.	2	4	-2				
x -	<i>y</i> =	7 ⇒	X =	y.	+ 7		
The	e tab	le fo	or x	= }	/ =	7 is	
X	5	11	9				

Now plotting the points on a graph and we get the following required graph:



The point at which the paths of the submarine and the destroyer intersect are (5, -2)

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